

## Economic and Environmental Dispatch at High Potential Solar Area with Renewable Storage

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**Abstract.** Economic/environmental dispatching (EED) is an important multiobjective optimization problem to decide the amount of generation to be allocated to each generating unit including renewable sources so that the total cost of generation and emission of polluting gases is minimized without violating system constraints. Here, the problem is EED of hybrid power system including solar, wind and storages of renewable energy. High potential renewable area ensures the availability of renewable sources to some extent. A consistent optimum EED can be obtained by extracting maximum renewable energy during its availability and using it for both available and unavailable periods with the aid of energy storage devices. This paper illustrates the optimization of EED with renewable storage using MATLAB simulations. The simulations have been performed using IEEE-30 test bus (with 6 generators) data.

**Keywords:** EED, multiobjective, renewable energy, solar energy, wind energy, energy storage, optimization.

### 1. Introduction

The power dispatch problem finds the optimum operating policy for committed generating units in order to meet the load demand while satisfying all unit and system equality and inequality constraints. Minimizing the fuel cost is the only one objective of the traditional economic dispatch (ED) problem. Due to the increased awareness about environmental issues, the utilities have been forced to use renewable sources with hybrid power systems and to modify their operation strategies in order to reduce the pollution and atmospheric emission of power plants. Economic/environmental dispatch (EED) is the proposed alternative for the same. It distributes active and renewable production among the power stations to meet the minimization of both fuel cost and pollutant emissions simultaneously [1, 2]. It is better to treat EED as multiobjective problems instead of treating it as single objective problem [3]. Several papers have described EED as multiobjective problem with solar or wind or both of these [1, 4].

Renewable energy resources depend on the climate data such as the wind speed, solar radiation, and temperature. The uncertainty and the variation of the renewable resources create challenges in EED problems. Different methodologies have been proposed to overcome these issues [1, 2]. One of the methods is to treat renewable power as a negative load and formulate demand equation on this basis [1, 5 & 6]. The uncertainty in the availability of solar irradiation is less in the high potential solar areas. Saudi Arabia is the one of the examples for such areas. The country is part of a vast, rainless region that receives about 6-7 kWh/m<sup>2</sup>/day with duration of sunshine of 7 - 9 hours. [7]. Other Middle East countries, some parts of India, Australia etc are also examples of high potential solar areas. The prediction of wind power at a particular location in a certain period of day is not possible due to the uncertainty of the wind speed. Wind does not blow at a point or steadily from one direction; it continues blowing from one point to another point. Installing number of

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inter connected wind turbines in the passage of wind will ensure the availability of wind power to some extent. Production and storage of renewable energy at off-peak times, and at times when there would be a surplus of its availability, and the reuse this stored energy during its unavailable periods will make the EED optimization more effective.

For traditional thermal generating units, the fuel cost increases with an increase of the output of the given thermal generating unit and amount of emission is also increases for higher values of output [8]. Thus, distributing the renewable energy throughout the operating period instead of using it only during its available period will help to reduce both cost and emission to some extent. Such a distribution can be achieved using suitable storage devices. In this paper, the EED is formulated as multiobjective problem with renewable sources and their storages. Discussion on renewable power is given in Section 2. The definitions and formulation of problems are described in section 3 and the results are presented and discussed in section 4.

## 2. Renewable Energy

In this paper, only solar and wind power is considered. Wind power is produced by wind turbines and solar power can be produced either by solar panels, by solar thermal plants, or by both. The maximum solar power produced by solar panels and the approximate solar power developed by solar thermal plant are proportional to solar irradiation ( $S \text{ W/m}^2$ ) and are given by equations (1) and (2) respectively

$$P_s = P_m \frac{S}{1000 \text{ W/s}} [1 - \tau(T_{cell} - 25)] \text{ W} \quad (1)$$

$$p_s = \eta A_c S \text{ W} \quad (2)$$

In equations (1) and (2),  $P_m$  is the panel power rating,  $\tau$  is the drift in panel temperature per  $^\circ\text{C}$ ,  $\eta$  is the collector efficiency and  $A_c$  is the collector area in  $\text{m}^2$ .

The mechanical power recovered by a wind turbine can be written as;

$$P_w = \frac{1}{2} a_c \rho A_s V_w^3 \text{ W} \quad (3)$$

where,  $a_c$  is the aerodynamic coefficient of wind turbine which depends on the turbine speed and wind speed,  $\rho$  is the air density,  $A_s$  is the surface swept in  $\text{m}^2$  and  $V_w$  is the wind speed in  $\text{m/s}^2$ .

In order to limit the variance in the useful power produced due to varying wind speed, the production of wind power is designed in such a way that it is constant for a certain range of wind speeds. Also, wind turbines are designed to develop a nominal Power  $P_n$  with a nominal wind speed  $V_n$ . Wind speed higher than  $V_n$  causes mechanical overloads in the turbine. To avoid mechanical overloading and to limit the variance in the developed power, the characteristic of wind power with wind speed is summarized in the table 1.

Table 1: Wind Power variation with Wind Speed

Wind Speed ( $V_w \text{ m/s}^2$ )	Wind Power ( $P_w \text{ W}$ )
$V_w \leq V_{\min}$	0
$V_{\min} < V_w < V_n$	Useful Power
$V_1 \leq V_w < V_2$	$P_{w1}$
$V_2 \leq V_w < V_3$	$P_{w2}$
$V_3 \leq V_w < V_n$	$P_{w3}$
$V_n \leq V_w \leq V_{\max}$	$P_n$
$V_w \geq V_{\max}$	0

where  $V_1$ ,  $V_2$  and  $V_3$  ( $V_{\min} < V_1 < V_2 < V_3 < V_n < V_{\max}$ ), are the different level of wind speed available per day and  $P_{w1}$ ,  $P_{w2}$  and  $P_{w3}$  are the corresponding values of useful power developed.

## 3. Problem Formulation

The main objective of EED is to minimize both fuel cost and the emissions of polluting gases by extracting maximum of power from the renewable sources. The objective functions are fuel cost function and emission function.

The fuel cost function  $F_f(P_{gi})$  in \$/h is represented by a quadratic equation such as;

$$F_f(P_{gi}) = \sum_{i=1}^{N_g} a_i + b_i P_{gi} + c_i P_{gi}^2 \quad (4)$$

In eqn. (4), the coefficients  $a_i$ ,  $b_i$  and  $c_i$  are the appropriate cost coefficients for individual generating units,  $P_{gi}$  is the real power output of the  $i^{\text{th}}$  generator and  $N_g$  is the number of the generators.

Main emissions in thermal power plants are  $\text{SO}_2$  and  $\text{NO}_x$ . The emission of  $\text{SO}_2$  depends on fuel consumption and has the same form as the fuel cost function. The emission of  $\text{NO}_x$  is related to many factors such as the temperature of the boiler and content of the air. The emission  $F_e(P_{gi})$  in ton/h of  $\text{SO}_2$  and  $\text{NO}_x$  pollutants is a function of generator output and can be expressed as,

$$F_e(P_{gi}) = \sum_{i=1}^{N_g} \alpha_i + \beta_i P_{gi} + \gamma_i P_{gi}^2 + \lambda_i e^{\delta_i P_{gi}} \quad (5)$$

In Eqn. (5), the coefficients  $\alpha_i$ ,  $\beta_i$ ,  $\gamma_i$ ,  $\lambda_i$  and  $\delta_i$  are emission coefficients of the  $i^{\text{th}}$  generating unit.

Wind with is available throughout the day at different locations with varying speed and sun light is available only for particular duration of the day. The aim is to extract maximum amount of power from solar reactor during its available period ( $T_a$ ). Some part of renewable power generated during this period is stored using some available storage devices. This stored power is delivered during unavailable period ( $T_u$ ) of sun light.

The power extracted from the renewable source is varying and can be considered as a variable load. Therefore this power ( $P_s + P_w$ ) is deducted from the total demand ( $P_D^t$ ) and also the stored power ( $P_{st}$ ) is added to it (during  $T_a$ ) or subtracted from it (during  $T_u$ ), to obtain the actual demand ( $P_D^a$ ), which is distributed among the available generating units. The net actual demand is expressed as,

$$P_D^a = P_D^t - (P_s + P_w)_g \pm P_{st} \quad (6)$$

In eqn. (6)  $P_s$  and  $P_w$  are solar and wind power generated respectively. Positive sign is applicable during the storage and negative sign is used during the delivering periods.

There are some constraints and these constraints are formulated as follows:

- The total power generation, renewable power that have to considered and stored power must cover the actual demand and the power loss ( $P_L$ ) in transmission lines so as to ensure power balance, i.e.
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$$P_D^a + P_L - \sum_{i=1}^{N_g} P_{gi} \quad (7)$$

- The generated real power of  $i^{\text{th}}$  unit is restricted by the lower limit  $P_{gi}^{\min}$  and the upper limit  $P_{gi}^{\max}$ .
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$$P_{gi}^{\min} \leq P_{gi} \leq P_{gi}^{\max}, \quad i=1, 2, \dots, N_g \quad (8)$$

- Active power loss of the transmission line is positive, i.e.,
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$$P_L > 0 \quad (9)$$

- The dispatched amount of renewable power is limited to some part ( $x$ ) of the total actual demand, i.e.
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$$(P_s + P_w) \geq x P_D^a \quad (10)$$

- The stored power is the difference of the total extracted and dispatched amount of renewable power during  $T_a$ . While, during  $T_u$ , it must not exceed some part ( $y$ ) of the total stored renewable power of  $T_a$  period. Moreover, the sum of total power delivered from the storage devices during  $T_u$  must not exceed the total power stored during  $T_a$ .

$$P_{st} \leq (P_s + P_w)_g - (P_s + P_w)_d ; \text{ during } T_a \quad (11)$$

And,

$$P_{st} \leq y \sum_{T_a} (P_s + P_w)_g - (P_s + P_w)_d ; \text{ during } T_u \quad (12)$$

where,  $y \propto \frac{T_a}{T_u} P_D^a$  in such a way that;

$$\sum_{T_u} P_{st} \leq \sum_{T_a} P_{st} \quad (13)$$

Now the optimization problem can be summarized as;

$$\text{Minimize } (F_f(P_{gi}), F_e(P_{gi}))$$

Subjected to the constrains given in equations (7) to (13)

The simulations of above multiobjective EED problem with given constraints were performed using MATLAB and the results are discussed next.

#### 4. Results and Discussions

The MATLAB simulations were carried out using the data of the standard IEEE 30 bus test system [1]. Here two case studies were considered: case A, during  $T_a$  and Case B, during  $T_u$ . Three sub cases such as; (1) without renewable & storage, (2) with renewable only and (3) with both renewable and storage were investigated. Let  $E_N$ ,  $E_R$  and  $E_{R\&S}$  are the values of emission per hour and  $C_N$ ,  $C_R$  and  $C_{R\&S}$  are the fuel cost per hour corresponding to these three sub cases. The values of the fuel and emission coefficients are given in Table 2. Lower and upper limits of generated active power of each generator are given as;

$$0.05 pu \leq P_{gi} \leq 1.5 pu ; i=1, 2, \dots, 6 \quad (14)$$

Table 2: Generator Cost and Emission Coefficients

	Cost			Emission			
	a	b	c	$\alpha$	$\beta$	$\gamma$	$\delta$
Pg1	10	200	100	4.091	-5.554	2x10-4	2.857
Pg2	10	150	120	2.543	-6.047	5x10-4	3.333
Pg3	20	180	40	4.258	-5.094	1x10-6	8
Pg4	10	100	60	5.326	-3.55	2x10-3	2
Pg5	20	180	40	4.258	-5.094	1x10-6	8
Pg6	10	150	100	6.131	-5.555	1x10-5	6.667

During  $T_a$  period, high intensity of solar radiation and wind with less or high speed is available and one must extract maximum power from the renewable source during this period. About 30% of total demand is dispatched from this extracted power and the remaining part is stored. Therefore both emission and cost are independent of stored energy during this period. Fig. 1 shows that,  $E_R$  decreases with increase in demand while  $E_N$  decreases upto a certain amount of demand and on further increase in demand it increases rapidly. Also  $C_R$  for a given demand is always less than  $C_N$ . The variation of emission with respect to cost is shown in Fig. 2. Comparing Fig. 1 & Fig. 2, it is clear that, 2.7 pu demand can be met with a cost of 400 \$/h with renewable sources while only 1.9 pu can meet without the renewable sources. However, the amount of emission is about 0.22 ton/h in both cases.

During  $T_u$ , both wind power and stored power are available. Due to the uncertainty of the wind speed, the dispatch amount of renewable power is less (about 20% total demand) as compared in case A. Considering 1 pu of stored power during this period, the dispatch amount of stored power is correlated to both demand and  $T_u$  duration. The results are summarized in Fig. 3 and Fig. 4. It is clear that, the fuel cost per hour is as  $C_{R\&S} < C_R < C_N$  for a given amount of demand and emission per hour is  $E_{R\&S} < E_R < E_N$  for higher values of demand.

Fig. 5 shows the percentage change in Cost (%  $\Delta C$ ) and Emission (%  $\Delta E$ ) for a given daily load curve. It is clear that more than 40% of fuel cost is saved during  $T_u$  with both storage & renewable sources, while the saving is less than 20% when only renewable sources are considered. And almost 35% of fuel cost can be saved during  $T_a$  with renewable sources. Also, the percentage change in emission is high for higher demand and it can be negative for lower demands.

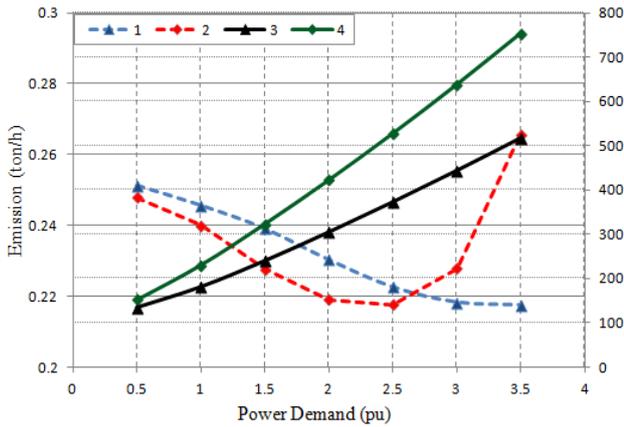


Fig. 1: Variation of Emission & Cost with Power Demand during  $T_u$ .  
1.  $E_R$ , 2.  $E_N$ , 3.  $C_R$  & 4.  $C_N$

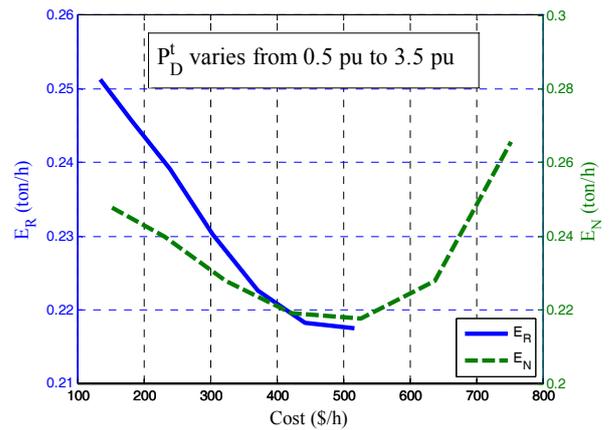


Fig. 2: Variation of Emission with Cost during T

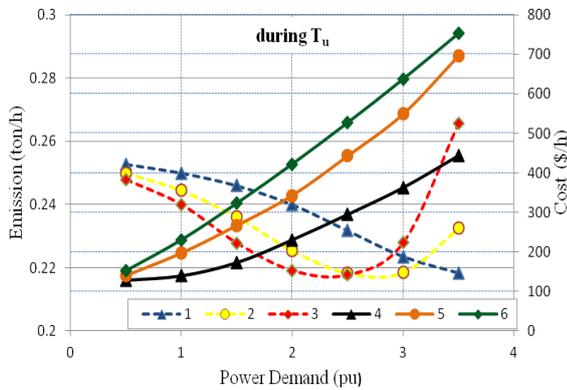


Fig. 3: Variations of Emission & Cost with Power Demand during  $T_u$ . 1.  $E_{R\&S}$ , 2.  $E_R$ , 3.  $E_N$ , 4.  $C_{R\&S}$ , 5.  $C_R$  & 6.  $C_N$

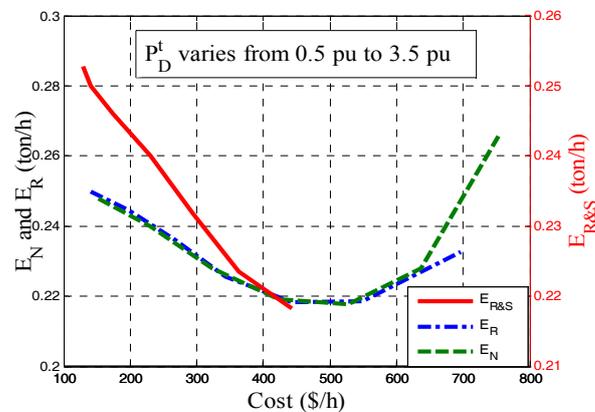


Fig. 4: Variation of Emission with Cost during T

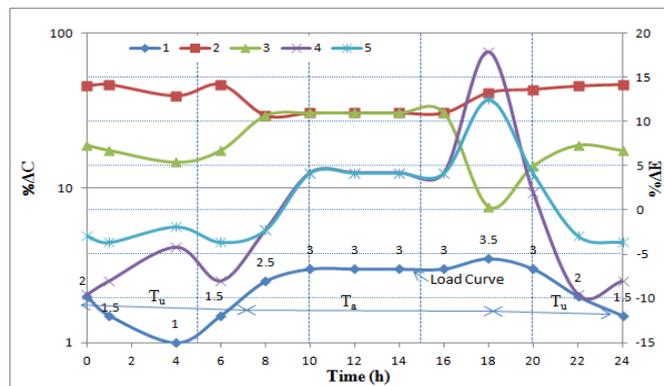


Fig. 5: Percentage change in Emission and Cost with Load Curve 1. Load (pu), 2. %  $\Delta C_{R\&S}$ , 3. %  $\Delta C_R$ , 4. %  $\Delta E_{R\&S}$  and 5. %  $\Delta E_R$

## 5. Conclusions

In this paper EED problem is formulated for a hybrid system which includes thermal generating units, solar, wind and renewable storage. Analysis is carried out using MATLAB simulation for a high irradiation solar region. Results show that, the renewable storage helps to extend advantage of clean energy sources into unavailable solar radiation periods. The optimized results are compared for both available and unavailable periods of sun light. From the analysis it is concluded that if less amount of extracted renewable power is required to optimal dispatch at low values of power demand, thereby large values of energy can be stored at low demand during the solar power available periods. High cost of storage device and uncertainty of renewable sources will reduce the reliability of this approach. Further research should be carried out in order to solve the problems related to the interconnection of number of renewable resources and to develop storage devices with lower cost.

## 6. References

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